BC Calc HW 1 - Functions

1. For each of the functions below, express the domain and range as sets of real numbers.

Example:

The function $a(x) = 2 + \sqrt{x-5}$ has domain $D = \{x \in \mathbb{R} \mid x \ge 5\}$ and range $R = \{y \in \mathbb{R} \mid y \ge 2\}$

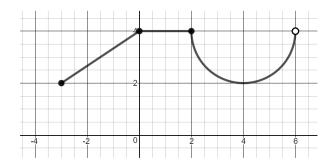
$$f(x) = 2x + 1$$

$$g(x) = x^2 - 3$$

$$h(x) = \frac{1}{2-x}$$

$$j(x) = \frac{1}{2}\sin(2x) + 3$$

2. Consider the graph y = f(x) below:



- a. Explain how you know this is the graph of a function.
- b. State the domain and range of f(x).
- c. Prove that this function is non-invertible by showing there exists two inputs that map to the same output.
- 3. Consider the example in problem 1 above. Suppose the range of a(x) were expressed as $R = \{x \in \mathbb{R} \mid x \ge 2\}$. Why might someone object to this? Why might someone argue that this is perfectly acceptable?